

CBCS SCHEME

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17MAT11

First Semester B.E. Degree Examination, June/July 2019

Engineering Mathematics - I

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing
ONE full question from each module.

Module-1

1. a. Find the n^{th} derivative of $\sin 2x \sin 3x$. (06 Marks)
 - b. Find the angle between the two curves $r = \frac{a}{1+\cos\theta}$ and $r = \frac{b}{1-\cos\theta}$ (07 Marks)
 - c. Find the radius of curvature for the curve $x^3 + y^3 = 3xy$ at $(3/2, 3/2)$. (07 Marks)
- OR**
2. a. If $y = \cos(m \log x)$ then prove that $x^2 y_{n+2} + (2n+1)xy_{n+1} + (m^2 + n^2)y_n = 0$. (06 Marks)
 - b. With usual notation prove that $\tan \phi = r \frac{d\theta}{dr}$. (07 Marks)
 - c. Find the pedal equation of the curve $r^m = a^m \cos m\theta$. (07 Marks)

Module-2

3. a. Find the Taylor's series of $\log(\cos x)$ in powers of $(x - \pi/3)$ upto fourth degrees terms. (06 Marks)
- b. If $u = \tan^{-1}\left(\frac{x^3 + y^3}{x + y}\right)$ then prove that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = \sin 2u$ by using Euler's theorem. (07 Marks)
- c. If $u = \frac{yz}{x}$, $v = \frac{xz}{y}$, $w = \frac{xy}{z}$ then find $J = \frac{\partial(uvw)}{\partial(xyz)}$. (07 Marks)

OR

4. a. Evaluate $\lim_{x \rightarrow 0} \left(\frac{\tan x}{x} \right)^{\frac{1}{x^2}}$. (06 Marks)
- b. Using Maclaurin's series, prove that $\sqrt{1 + \sin 2x} = 1 + x - \frac{x^2}{2} - \frac{x^3}{3} + \frac{x^4}{4} - \dots$. (07 Marks)
- c. If $u = f(2x - 3y, 3y - 4z, 4z - 2x)$ then prove that $\frac{1}{2} \frac{\partial u}{\partial x} + \frac{1}{3} \frac{\partial u}{\partial y} + \frac{1}{4} \frac{\partial u}{\partial z} = 0$. (07 Marks)

Module-3

5. a. A particle moves along the cuvre $\vec{r} = (t^3 - 4t)\hat{i} + (t^2 + 4t)\hat{j} + (8t^2 - 3t^3)\hat{k}$. Find the components of velocity and acceleration in the direction of $\hat{i} - 3\hat{j} + 2\hat{k}$ at $t = 0$. (06 Marks)
- b. Find the constant a and b such that $\vec{F} = (axy + z^3)\hat{i} + (3x^2 - z)\hat{j} + (bxz^2 - y)\hat{k}$ is irrotational and find scalar potential function ϕ such that $\vec{F} = \nabla\phi$. (07 Marks)
- c. Prove that $\text{curl}(\phi \vec{A}) = \phi \text{curl} \vec{A} + \text{grad} \phi \times \vec{A}$. (07 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.



17MAT11

OR

- 6 a. Show that vector field $\mathbf{F} = \frac{x\hat{i} + y\hat{j}}{x^2 + y^2}$ is both solenoidal and irrotational. (06 Marks)
- b. If $\vec{F} = (x+y+1)\hat{i} + \hat{j} - (x+y)\hat{k}$ then prove that $\vec{F} = \text{curl } \vec{F} = 0$. (07 Marks)
- c. Show that $\text{div}(\text{curl } \vec{A}) = 0$. (07 Marks)

Module-4

- 7 a. Obtain reduction formula for $\int \sin^n x dx$ ($n > 0$). (06 Marks)
- b. Solve the differential equation $\frac{dy}{dx} + y \cot x = \cos x$. (07 Marks)
- c. Find the orthogonal trajectory of the curve $r = a(1 + \sin \theta)$. (07 Marks)

OR

- 8 a. Evaluate $\int_0^{\frac{\pi}{2}} \sin^7 \theta \cos^6 \theta d\theta$. (06 Marks)
- b. Solve the differential equation : $(2xy + y - \tan y)dx + (x^2 - x \tan^2 y + \sec^2 y)dy = 0$. (07 Marks)
- c. If the temperature of air is 30°C and the substance cools from 100°C to 70°C in 15 mins. Find when the temperature will be 40°C . (07 Marks)

Module-5

- 9 a. Find the rank of the matrix $\begin{bmatrix} 1 & 1 & 1 & 6 \\ 1 & -1 & 2 & 5 \\ 3 & 1 & 1 & 8 \\ 2 & -2 & 3 & 7 \end{bmatrix}$ by reducing to Echelon form. (06 Marks)
- b. Find the largest eigen value and eigen vector of the matrix : $\begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$ by taking initial vector as $[1 \ 1 \ 1]^T$ by using Rayleigh's power method. Carry out five iteration. (07 Marks)
- c. Reduce $8x^2 + 7y^2 + 3z^2 - 12xy + 4xz - 8yz$ into canonical form, using orthogonal transformation. (07 Marks)

OR

- 10 a. Solve the system of equations
 $10x + y + z = 12$
 $x + 10y + z = 12$
 $x + y + 10z = 12$
 by using Gauss-Seidel method. Carry out three iterations. (06 Marks)
- b. Diagonalise the matrix $A = \begin{bmatrix} 5 & 4 \\ 1 & 2 \end{bmatrix}$. (07 Marks)
- c. Show that the transformation
 $y_1 = x_1 + 2x_2 + 5x_3$
 $y_2 = 2x_1 + 4x_2 + 11x_3$
 $y_3 = -x_2 + 2x_3$
 is regular. Write down inverse transformation. (07 Marks)