

# CBCS SCHEME



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15MATDIP31

Third Semester B.E. Degree Examination, June/July 2019

## Additional Mathematics – I

Time: 3 hrs.

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

### Module-1

- Express the complex number  $\frac{(1+i)(1+3i)}{1+5i}$  in the form  $a + ib$ . (05 Marks)
  - Find the modulus and amplitude of  $1 + \cos \theta + i \sin \theta$ . (05 Marks)
  - Show that  $(a + ib)^n + (a - ib)^n = 2(a^2 + b^2)^{n/2} \cos \left( n \tan^{-1} \left( \frac{b}{a} \right) \right)$  (06 Marks)

OR

- If  $\vec{A} = i - 2j + 3k$  and  $\vec{B} = 2i + j + k$ , find the unit vector perpendicular to both  $\vec{A}$  and  $\vec{B}$ . (05 Marks)
  - Show that the points  $-6i + 3j + 2k$ ,  $3i - 2j + 4k$ ,  $5i + 7j + 3k$  and  $-13i + 17j - k$  are coplanar. (05 Marks)
  - Prove that  $\left[ \vec{B} \times \vec{C}, \vec{C} \times \vec{A}, \vec{A} \times \vec{B} \right] = \left[ \vec{A} \vec{B} \vec{C} \right]^2$  (06 Marks)

### Module-2

- Find the  $n^{\text{th}}$  derivative of  $\frac{x}{(x-1)(2x+3)}$ . (05 Marks)
  - Find the angle of intersection of the curves  $r = a(1 + \cos \theta)$  and  $r = b(1 - \cos \theta)$ . (05 Marks)
  - Obtain the Maclourin series expansion of the function  $\sin x$  upto the term containing  $x^4$ . (06 Marks)

OR

- Show that  $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 2u \log u$  where  $\log u = \frac{x^3 + y^3}{3x + 4y}$ . (05 Marks)
  - If  $u = f(x - y, y - z, z - x)$  prove that  $\frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z} = 0$ . (05 Marks)
  - If  $u = x + 3y^2 - z^3$ ,  $v = 4x^2yz$ ,  $w = 2z^2 - xy$ , evaluate  $\frac{\partial(u, v, w)}{\partial(x, y, z)}$  at  $(1, -1, 0)$ . (06 Marks)

### Module-3

- Obtain the reduction formula for  $\int \sin^n x \, dx$ . Hence evaluate  $\int_0^{\pi/2} \sin^n x \, dx$ . (05 Marks)
  - Evaluate  $\int_0^8 \frac{x^6}{(1+x^2)^7} \, dx$ . (05 Marks)
  - Evaluate  $\int_{-1}^1 \int_0^z \int_{x-z}^{x+z} (x + y + z) \, dx \, dy \, dz$ . (06 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8=50, will be treated as malpractice.



15MATDIP31

OR

- 6 a. Evaluate  $\int_0^{2a} \int_0^{x^2/4a} xy dy dx$ . (05 Marks)
- b. Evaluate  $\int_0^1 \int_0^1 \int_0^1 (x+y+z) dx dy dz$ . (05 Marks)
- c. Evaluate  $\int_0^a \frac{x^7 dx}{\sqrt{a^2-x^2}}$  by using reduction formula. (06 Marks)

**Module-4**

- 7 a. A particle moves along the curve  $x = t^3 + 1$ ,  $y = t^2$ ,  $z = 2t + 3$  where  $t$  is the time. Find the components of velocity and acceleration at  $t = 1$  in the direction of  $i + j + 3k$ . (05 Marks)
- b. Find  $\text{div} \vec{F}$  and  $\text{curl} \vec{F}$  where  $\vec{F} = \text{grad}(x^3 + y^3 + z^3 - 3xyz)$ . (05 Marks)
- c. Prove that  $\text{div}(\text{curl} \vec{F}) = 0$ . (06 Marks)

OR

- 8 a. Find the directional derivative of  $f(x, y, z) = xy^3 + yz^3$  at  $(2, -1, 1)$  in the direction of  $i + 2j + 2k$ . (08 Marks)
- b. Prove that  $\nabla^2 \left( \frac{1}{r} \right) = 0$  where  $r = \sqrt{x^2 + y^2 + z^2}$ . (08 Marks)

**Module-5**

- 9 a. Solve  $(x^2 - y^2)dx - xy dy = 0$ . (05 Marks)
- b. Solve  $\left[ y \left( 1 + \frac{1}{x} \right) + \cos y \right] dx + (x + \log x - x \sin y) dy = 0$ . (05 Marks)
- c. Solve  $\frac{dy}{dx} - \frac{y}{1+x} = e^{3x}(x+1)$ . (06 Marks)

OR

- 10 a. Solve  $(xy^3 + y)dx + 2(x^2y^2 + x + y^4)dy = 0$ . (08 Marks)
- b. Solve  $(3y + 2x + 4)dx - (4x + 6y + 5)dy = 0$ . (08 Marks)

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