





14MAT21

- 6 a. Evaluate  $\int_0^1 \int_0^{\sqrt{1-x^2}} \int_0^{\sqrt{1-x^2-y^2}} xyz dz dy dx$ . (06 Marks)
- b. Solve PDE by direct integration method.  $\frac{\partial^2 z}{\partial x \partial t} = e^{-t} \cos x$  given  $z=0$  when  $t=0$  and  $\frac{\partial z}{\partial t} = 0$  when  $x=0$ . (07 Marks)
- c. Obtain solution of one dimensional wave equation,  $\frac{\partial^2 y}{\partial t^2} = C^2 \frac{\partial^2 y}{\partial x^2}$  by the method of separation of variables. (07 Marks)

**Module – 4**

- 7 a. Find the area between parabolas  $y^2 = 4ax$  and  $x^2 = 4ay$ . (06 Marks)
- b. Show that  $\int_0^{\frac{\pi}{2}} \frac{d\theta}{\sqrt{\sin \theta}} \int_0^{\frac{\pi}{2}} \sqrt{\sin \theta} d\theta = \pi$ . (07 Marks)
- c. Prove that cylindrical coordinates system is orthogonal. (07 Marks)
- 8 a. Evaluate  $\int_0^1 x^6 (1-x^2)^{\frac{1}{2}} dx$ . (06 Marks)
- b. Express the vector  $zi - 2xj + yk$  in cylindrical co-ordinates. (07 Marks)
- c. Find the volume bounded by the surface  $z^2 = a^2 - x^2$  and the planes  $x=0, y=0, z=0$  and  $y=b$ . (07 Marks)

**Module – 5**

- 9 a. Find Laplace transform of,  
(i)  $te^{-t} \sin(4t)$  (ii)  $\frac{\cos at - \cos bt}{t}$ . (06 Marks)
- b. Find inverse Laplace transform of  $\frac{5s+3}{(s-1)(s^2+2s+5)}$ . (07 Marks)
- c. Express the function,  $f(t) = \begin{cases} \pi - t & 0 < t < \pi \\ \sin t & t > \pi \end{cases}$  in terms of unit step function and hence find its Laplace transform. (07 Marks)
- 10 a. Find inverse Laplace transform of the following using convolution theorem  $L^{-1} \left[ \frac{s}{(s-1)(s^2+4)} \right]$ . (06 Marks)
- b. Given  $f(t) = \begin{cases} E & 0 < t < \frac{a}{2} \\ -E & \frac{a}{2} < t < a \end{cases}$  where  $f(t+a) = f(t)$ . Show that  $L\{f(t)\} = \frac{E}{S} \tanh\left(\frac{aS}{2}\right)$ . (07 Marks)
- c. Using Laplace transform method, solve  $\frac{d^2 y}{dt^2} + 6 \frac{dy}{dt} + 9y = 12t^2 e^{-3t}$ . (07 Marks)

\* \* \* \* \*