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14MAT11

First Semester B.E. Degree Examination, June/July 2017
Engineering Mathematics – I

Time: 3 hrs.

Max. Marks:100

Note: Answer any FIVE full questions, selecting at least ONE question from each part.

Module-1

- 1 a. Find the n^{th} derivative of $y = \sin^2 x \sin h^2 x + \log_{10} (x^2 - 3x + 2)$. (07 Marks)
- b. Find the pedal equation for the curve $r = a + b \cos \theta$. (06 Marks)
- c. Obtain radius of curvature for the parametric curve, $x = a(t - \sin t)$ $y = a(1 - \cos t)$. (07 Marks)

- 2 a. If $y = \tan^{-1} x$, prove that $(1 + x^2)y_{n+2} + 2(n + 1)xy_{n+1} + n(n + 1)y_n = 0$. Hence obtain $y_n(0)$. (07 Marks)
- b. Find the angle of intersection between the curves $r = 2 \sin \theta$; $r = 2(\sin \theta + \cos \theta)$. (06 Marks)
- c. Find the radius of curvature for the polar curve $r^2 = a^2 \cos 2 \theta$. (07 Marks)

Module-2

- 3 a. Evaluate : $\lim_{x \rightarrow 0} (\cos x)^{\cot^2 x}$. (06 Marks)
- b. Determine Maclarin's series for the function for $f(x) = \log (1 + \cos x)$ upto term containing x^4 . (07 Marks)
- c. If $u = f(2x - 3y, 3y - 4z, 4z - 2x)$ then obtain the value of $\frac{1}{2} \frac{\partial u}{\partial x} + \frac{1}{3} \frac{\partial u}{\partial y} + \frac{1}{4} \frac{\partial u}{\partial z}$. (07 Marks)

- 4 a. Find total derivative of u with respect to t where $u = \tan^{-1} x/y$, $x = e^t - e^{-t}$, $y = e^t + e^{-t}$. (06 Marks)
- b. If $u = \frac{x}{y-z}$, $v = \frac{y}{z-x}$, $w = \frac{z}{x-y}$, find the Jacobian $\frac{\partial(u, v, w)}{\partial(x, y, z)}$. Determine whether u , v and w are functionally dependent. (07 Marks)
- c. If x y z be the angles of a triangle, show that the maximum value of $\sin x \sin y \sin z$ is $\frac{3\sqrt{3}}{8}$. (07 Marks)

Module-3

- 5 a. A particle moves along $x = t^3 - 4t$, $y = t^2 + 4t$, $z = 8t^2 - 3t^3$, where 't' denotes time. Find the magnitudes of velocity and acceleration at time $t = 2$. (07 Marks)
- b. Assuming the validity of differentiation under integral sign prove that $\int_0^{\infty} e^{-x^2} \cos \alpha x dx = \frac{\sqrt{\pi}}{2} e^{-\alpha^2/4}$. (07 Marks)
- c. Trace the curve $x^{2/3} + y^{2/3} = a^{2/3}$, using general rules of tracing the curve. (06 Marks)



- 6 a. If $\vec{F} = \text{grad}(x^3 + y^3 + z^3 - 3xyz)$ find $\text{curl } \vec{F}$. Is \vec{F} irrotational? (07 Marks)
- b. Prove that if \vec{F} is a vector point function $\text{div}(\text{curl } \vec{F}) = 0$. (07 Marks)
- c. If \vec{r} is a position vector of a point in space obtain $\text{div } \vec{r}$ and $\text{curl } \vec{r}$. (06 Marks)

Module-4

- 7 a. Solve $\frac{dy}{dx} + x \sin 2y = x^3 \cos^2 y$. (07 Marks)
- b. Obtain the reduction formula for $\int_0^{\pi/2} \cos^n x \, dx$, where 'n' is a positive integer. (07 Marks)
- c. A body originally at 80°C cools down to 60°C in 20 minutes, the temperature of air being 40°C . What will be the temperature of the body after 40 minutes from the original? (06 Marks)
- 8 a. Show that family $\frac{x^2}{a^2 + \lambda} + \frac{y^2}{b^2 + \lambda} = 1$ with λ as a parameter is self orthogonal. (07 Marks)
- b. Evaluate: $\int_0^{2a} x^3 \sqrt{2ax - x^2} \, dx$. (07 Marks)
- c. Solve: $(y^2 e^{xy^2} + 4x^3) dx + (2xy e^{xy^2} + 3y^2) dy = 0$. (06 Marks)

Module-5

- 9 a. Solve by gauss elimination method:
 $2x - 3y + 4z = 7$
 $5x - 2y + 2z = 7$
 $6x - 3y + 10z = 23$. (07 Marks)
- b. Reduce the quadratic form: $3x_1^2 + 3x_2^2 + 3x_3^2 + 2x_1x_2 + 2x_1x_3 - 2x_2x_3$ into canonical form by orthogonal transformation. (07 Marks)
- c. Find the largest eigen value and corresponding eigen vector by Rayleigh's power method performing five iterations, with $x^{(0)} = [1, 1, 1]^T$ for $A = \begin{bmatrix} 1 & 6 & 1 \\ 1 & 2 & 0 \\ 0 & 0 & 3 \end{bmatrix}$. (06 Marks)
- 10 a. Solve by LU decomposition method:
 $10x + y + z = 12$
 $2x + 10y + z = 13$
 $2x + 2y + 10z = 14$. (07 Marks)
- b. Diagonalize the matrix $A = \begin{bmatrix} -1 & 3 \\ -2 & 4 \end{bmatrix}$. Hence find A^4 . (07 Marks)
- c. Solve by Gauss Seidel iteration method:
 $20x + y - 2z = 17$
 $3x + 20y - z = -18$
 $2x - 3y + 20z = 25$
Perform 3 iterations. (06 Marks)
