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14MAT11

First Semester B.E. Degree Examination, June/July 2015

Engineering Mathematics - I

Time: 3 hrs.

Max. Marks:100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

MODULE - I

- 1 a. If $y^{1/m} + y^{-1/m} = 2x$ prove that
 $(x^2 - 1)y_{n+2} + (2n + 1)xy_{n+1} + (n^2 - m^2)y_n = 0$ (07 Marks)
- b. Find the pedal equation for the curve
 $r^m = a^m \sin m\theta + b^m \cos m\theta$ (06 Marks)
- c. Derive an expression to find radius of curvature in cartesian form. (07 Marks)

OR

- 2 a. Find the n^{th} derivative of $\sin^2 x \cos^3 x$ (07 Marks)
- b. Show that the curves $r = a(1 + \cos \theta)$ and $r = b(1 - \cos \theta)$ intersect at right angles. (06 Marks)
- c. Find the radius of curvature when $x = a \log(\sec \theta + \tan \theta)$, $y = a \sec \theta$. (07 Marks)

MODULE - II

- 3 a. Using Maclaurin's series expand $\tan x$ upto the term containing x^5 . (07 Marks)
- b. Show that $x \frac{\partial u}{\partial x} + y \frac{\partial u}{\partial y} = 2u \log u$ where $\log u = \frac{x^3 + y^3}{3x + 4y}$ (06 Marks)
- c. Find the extreme values of $x^4 + y^4 - 2(x - y)^2$ (07 Marks)

OR

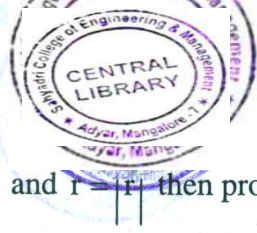
- 4 a. Evaluate $\lim_{x \rightarrow 0} \left\{ \frac{e^x \sin x - x - x^2}{x^2 + x \log(1 - x)} \right\}$ (07 Marks)
- b. If $u = x \log xy$ where $x^3 + y^3 + 3xy = 1$ Find $\frac{du}{dx}$ (06 Marks)
- c. If $u = \frac{yz}{x}$, $v = \frac{xz}{y}$, $w = \frac{xy}{z}$, find $\frac{\partial(u, v, w)}{\partial(x, y, z)}$. (07 Marks)

MODULE - III

- 5 a. Find $\text{div } \vec{F}$ and $\text{Curl } \vec{F}$ where
 $\vec{F} = \text{grad}(x^3 + y^3 + z^3 - 3xyz)$ (07 Marks)
- b. Using differentiation under integral sign,
 Evaluate $\int_0^1 \frac{x^\alpha - 1}{\log x} dx$ ($\alpha \geq 0$)
 Hence find $\int_0^1 \frac{x^3 - 1}{\log x} dx$ (06 Marks)
- c. Trace the curve $y^2(a - x) = x^3$, $a > 0$ use general rules. (07 Marks)

OR

Important Note : 1. On completing your answers, compute by draw diagonal cross lines on the remaining blank part.
 2. Any revealing of identification, appeal to evaluator and/or equations written eg. 42+8 = 50, will be treated as malpractice.



- 6 a. If $\vec{r} = xi + yj + zk$ and $r = |\vec{r}|$ then prove that $\nabla r^n = nr^{n-2} \vec{r}$ (07 Marks)
- b. Find the constants a, b, c such that $\vec{F} = (x + y + az)i + (bx + 2y - z)j + (x + cy + 2z)k$ is irrotational. Also find ϕ such that $\vec{F} = \nabla\phi$ (06 Marks)
- c. Using differentiation under integral sign,
Evaluate $\int_0^\infty e^{-ax} \frac{\sin x}{x} dx$ (07 Marks)

MODULE- IV

- 7 a. Obtain reduction formula for $\int_0^{\pi/2} \cos^n x dx$ (07 Marks)
- b. Solve : $(1 + 2xy \cos x^2 - 2xy)dx + (\sin x^2 - x^2)dy = 0$ (06 Marks)
- c. A body originally at 80°C cools down to 60°C in 20 minutes, the temperature of the air being 40°C. What will be temperature of the body after 40 minutes from the original? (07 Marks)

OR

- 8 a. Evaluate $\int_0^{2a} x^2 \sqrt{2ax - x^2} dx$ (07 Marks)
- b. Solve : $xy(1 + x y^2) \frac{dy}{dx} = 1$ (06 Marks)
- c. Find the orthogonal trajectories of the family of confocal conics $\frac{x^2}{a^2} + \frac{y^2}{b^2 + \lambda} = 1$ where λ is parameter. (07 Marks)

MODULE- V

- 9 a. Solve by Gauss elimination method
 $5x_1 + x_2 + x_3 + x_4 = 4, x_1 + 7x_2 + x_3 + x_4 = 12, x_1 + x_2 + 6x_3 + x_4 = -5,$
 $x_1 + x_2 + x_3 + 4x_4 = -6$ (07 Marks)
- b. Diagonalize the matrix $A = \begin{bmatrix} -19 & 7 \\ -42 & 16 \end{bmatrix}$ (06 Marks)
- c. Find the dominant eigen value and the corresponding eigen vector of the matrix
 $A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$
by power method taking the initial eigen vector $(1, 1, 1)^T$ (07 Marks)

OR

- 10 a. Solve by L U decomposition method
 $x + 5y + z = 14, 2x + y + 3z = 14, 3x + y + 4z = 17$ (07 Marks)
- b. Show that the transformation $y_1 = 2x_1 - 2x_2 - x_3, y_2 = -4x_1 + 5x_2 + 3x_3,$
 $y_3 = x_1 - x_2 - x_3$ is regular and find the inverse transformation. (06 Marks)
- c. Reduce the quadratic form $2x_1^2 + 2x_2^2 + 2x_3^2 + 2x_1x_3$ into canonical form by orthogonal transformation. (07 Marks)
