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10MAT31

Third Semester B.E. Degree Examination, June/July 2015

Engineering Mathematics - III

Time: 3 hrs.

Max. Marks: 100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

PART - A

1 a. Expand f(x) = x sin x as a Fourier series in the interval (-pi, pi), Hence deduce the following:

i) pi/2 = 1 + 2/1.3 - 2/3.5 + 2/5.7

ii) (pi-2)/4 = 1/1.3 - 1/3.5 + 1/5.7 - + ...

(07 Marks)

b. Find the half-range Fourier cosine series for the function

f(x) = { kx, 0 <= x <= l/2; k(l-x), l/2 < x <= l

Where k is a non-integer positive constant.

(06 Marks)

c. Find the constant term and the first two harmonics in the Fourier series for f(x) given by the following table.

Table with 2 rows: x and F(x) and 8 columns of values.

(07 Marks)

2 a. Find the Fourier transform of the function f(x) = xe^{-ax}

(07 Marks)

b. Find the Fourier sine transforms of the

Functions f(x) = { sin x, 0 < x < a; 0, x >= a

(06 Marks)

c. Find the inverse Fourier sine Transform of

F_x(alpha) = 1/alpha * e^{-a*alpha} a > 0.

(07 Marks)

3 a. Find various possible solution of one dimensional wave equation d^2u/dt^2 = C^2 * d^2u/dx^2 by separable variable method. (07 Marks)

b. Obtain solution of heat equation du/dt = C^2 * d^2u/dx^2 subject to condition u(0,t) = 0, u(l,t) = 0, u(x,0) = f(x). (06 Marks)

c. Solve Laplace equation d^2u/dx^2 + d^2u/dy^2 = 0 subject to condition u(0,y) = u(l,y) = 0, u(x,0) = 0, u(x,a) = sin(pi*x/l). (07 Marks)

Important Note : 1. On completing your answers, carefully draw diagonal cross lines on the remaining blank page. 2. Any revealing of identification, appeal to evaluator and/or equations written eg. 42+8 = 50, will be treated as malpractice.



- 4 a. The pressure P and volume V of a gas are related by the equation $PV^r = K$, where r and K are constants. Fit this equation to the following set of observations (in appropriate units)

P :	0.5	1.0	1.5	2.0	2.5	3.0
V :	1.62	1.00	0.75	0.62	0.52	0.46

(07 Marks)

- b. Solve the following LPP by using the Graphical method :

Maximize : $Z = 3x_1 + 4x_2$

Under the constraints $4x_1 + 2x_2 \leq 80$

$2x_1 + 5x_2 \leq 180$

$x_1, x_2 \geq 0$.

(06 Marks)

- c. Solve the following using simplex method

Maximize : $Z = 2x + 4y$, subject to the

Constraint : $3x + y \leq 2z$, $2x + 3y \leq 24$, $x \geq 0$, $y \geq 0$.

(07 Marks)

PART - B

- 5 a. Using the Regular - Falsi method, find a real root (correct to three decimal places) of the equation $\cos x = 3x - 1$ that lies between 0.5 and 1 (Here, x is in radians). (07 Marks)

- b. By relaxation method

Solve : $-x + 6y + 27z = 85$, $54x + y + z = 110$, $2x + 15y + 6z = 72$. (06 Marks)

- c. Using the power method, find the largest eigen value and corresponding eigen vectors of the

matrix $A = \begin{bmatrix} 6 & -2 & 2 \\ -2 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$

taking $[1, 1, 1]^T$ as the initial eigen vectors. Perform 5 iterations. (07 Marks)

- 6 a. From the data given in the following Table ; find the number of students who obtained (i) Less than 45 marks (ii) between 40 and 45 marks.

Marks	30 - 40	40 - 50	50 - 60	60 - 70	70 - 80
No. of Students	31	42	51	35	31

(07 Marks)

- b. Using the Lagrange's formula, find the interpolating polynomial that approximates to the function described by the following table:

x	0	1	2	3	4
f(x)	3	6	11	18	27

Hence find $f(0.5)$ and $f(3.1)$. (06 Marks)

- c. Evaluate $\int_0^1 \frac{x}{1+x^2} dx$ by using Simpson's $\left(\frac{3}{8}\right)^{th}$ Rule, dividing the interval into 3 equal parts.

Hence find an approximate value of $\log \sqrt{2}$. (07 Marks)

- 7 a. Solve the one - dimensional wave equation $\frac{\partial^2 u}{\partial x^2} = \frac{\partial^2 u}{\partial t^2}$

Subject to the boundary conditions $u(0, t) = 0$, $u(1, t) = 0$, $t \geq 0$ and the initial conditions

$u(x, 0) = \sin \pi x$, $\frac{\partial u}{\partial t}(x, 0) = 0$, $0 < x < 1$. (07 Marks)



b. Consider the heat equation $2 \frac{\partial^2 u}{\partial x^2} = \frac{\partial u}{\partial t}$ under the following conditions:

i) $u(0, t) = u(4, t) = 0, t \geq 0$

ii) $u(x, 0) = x(4 - x), 0 < x < 4.$

Employ the Bendre - Schmidt method with $h = 1$ to find the solution of the equation for $0 < t \leq 1.$ (06 Marks)

c. Solve the two - dimensional Laplace equation $\frac{\partial^2 u}{\partial x^2} = \frac{\partial^2 u}{\partial y^2} = 0$ at the interior pivotal points of the square region shown in the following figure. The values of u at the pivotal points on the boundary are also shown in the figure. (07 Marks)

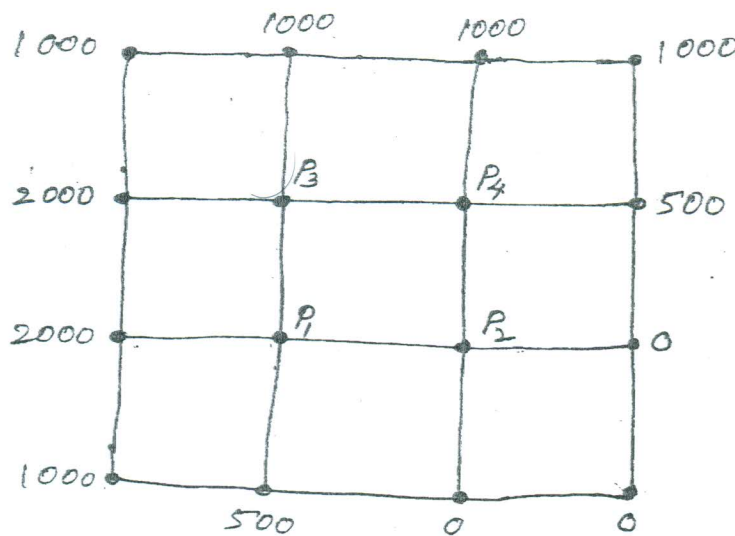


Fig. Q7 (c)

8 a. State and prove the recurrence relation of Z - Transformation hence find $Z_T(n^p)$ and

$Z_T \left[\cosh \left(\frac{n\pi}{2} + \theta \right) \right].$ (07 Marks)

b. Find $Z_T^{-1} \left[\frac{z^3 - 20z}{(z-2)^3(z-4)} \right]$ (06 Marks)

c. Solve the difference equation

$y_{n+2} - 2y_{n+1} - 3y_n = 3^n + 2n$

Given $y_0 = y_1 = 0.$

(07 Marks)
