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**Second Semester B.E. Degree Examination, June/July 2017**  
**Engineering Mathematics – II**

Time: 3 hrs.

Max. Marks: 100

**Note: 1. Answer any FIVE full questions, choosing at least two from each part.****2. Answer all objective type questions on any single page of the answer booklet.****PART – A****1 a. Choose the correct answers for the following : (04 Marks)**i) Solution of one of the factors of  $p^2 - p - 1 = 0$  with  $p = \frac{dy}{dx}$  is  $y = \underline{\hspace{2cm}}$ .

A)  $\left(\frac{1+\sqrt{5}}{2}\right)x^4 + C$ , B)  $\left(\frac{2+\sqrt{5}}{2}\right)x^3 + C$  C)  $\left(\frac{2-\sqrt{5}}{2}\right)x^2 + C$  D)  $\left(\frac{1-\sqrt{5}}{2}\right)x + C$

ii) On solving for  $x$  in  $P = \tan\left(x - \frac{P}{1+P^2}\right)$  the solution for  $y = \underline{\hspace{2cm}}$ .

A)  $C + \frac{1}{1+P^2}$  B)  $C - \frac{2}{1+P^2}$  C)  $C - \frac{3}{1+P^2}$  D)  $C - \frac{1}{1+P^2}$

iii) The solution for Clairut's form of the differential equation,  $(y - Px)(P - 1) = P$  is  $y = \underline{\hspace{2cm}}$ .

A)  $Cx - \frac{C}{C-1}$  B)  $Cx + \frac{C}{C-1}$  C)  $C^2 - \frac{Cx}{C-1}$  D)  $C^2 + \frac{Cx}{C-1}$

iv) If the given equation is solvable for  $y$  then it is of the form,

A)  $y = f(x, p)$  B)  $x = f(y, p)$  C)  $x = f(y/p)$  D)  $x = f(p/y)$

b. Solve  $xyp^2 + p(3x^2 - 2y^2) - 6xy = 0$  with solvable for  $P$ . (05 Marks)c. Solve  $(px - y)(py + x) = \alpha^2 p$  with  $x^2 = u$  and  $y^2 = v$  using Clairut's form. (05 Marks)d. Solve  $y = x + a \tan^{-1} p$ . (06 Marks)**2 a. Choose the correct answers for the following : (04 Marks)**i) Solution of  $(D^3 - 2D + 4)y = 0$  is  $y = \underline{\hspace{2cm}}$ .

A)  $C_1 e^{2x} + C_2 e^{-x} \cos x + C_3 e^{-x} \sin x$  B)  $C_1 e^{2x} + C_2 e^{-x} \cos x$   
 C)  $C_1 e^{-2x} + C_2 e^x \cos x + C_3 e^x \sin x$  D)  $C_1 \cos x + C_2 \sin x$

ii) Particular integral of  $(D^2 + 1)y = \sin 2x$  is  $y_p = \underline{\hspace{2cm}}$ .

A)  $\frac{1}{3} \sin 2x$  B)  $\sin 2x$  C)  $\cos 2x$  D)  $-\frac{1}{3} \sin 2x$

iii) Particular integral of  $(D - 1)y = \sinh x$  is  $y = \underline{\hspace{2cm}}$ .

A)  $\frac{1}{2}(xe^x + e^{-x})$  B)  $\frac{1}{2}xe^{-x}$  C)  $\frac{1}{2}(e^{-x} + e^x)$  D)  $\frac{1}{2}$

iv) The displacement in the simple harmonic motion  $\frac{d^2x}{dt^2} = -\mu^2 x$  is  $\underline{\hspace{2cm}}$ .

A)  $C_1 \cos \mu t - C_2 \sin \mu t$  B)  $C_1 \cos \mu t + C_2 \sin \mu t$   
 C)  $C_1 \cos t + C_2 \sin t$  D)  $C_1 \cos t - C_2 \sin t$

b. Solve  $(D^2 - 6D + 13)y = 8e^{3x} \sin 4x + 2^x$ . (05 Marks)c. Solve  $y'' - 2y' + y = xe^x \sin x$ . (05 Marks)d. Solve  $(D + 3)x + (D + 1)y = e^t$  and  $(D + 1)x + (D - 1)y = t$ . (06 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.  
 2. Any revealing of identification, appeal to evaluator and/or equations written eg. 42+8 = 50, will be treated as malpractice.

- 3 a. Choose the correct answers for the following : (04 Marks)
- i) Particular solution of  $(D^2 - 1)y = 1$  using variation of parameters is  $y_p = \underline{\hspace{2cm}}$ .  
 A)  $-1$                       B)  $-2$                       C)  $-3$                       D)  $-4$
- ii) The differential equation,  $x^3 y''' + x^2 y'' = \log x$  reduces to the form when  $x = e^t$  as,  
 A)  $(D+1)^3 y = t$       B)  $D(D-1)^2 y = t$       C)  $D^3 y = 0$               D)  $D^2 y = 0$
- iii) The complementary function of,  $(1+x)^2 y'' + (1+x)y' + y = 2 \sin \log(x+1)$  with  $(1+x) = e^t$  is  $y_c = \underline{\hspace{2cm}}$ .  
 A)  $C_1 \cos t - C_2 \sin t$                       B)  $C_1 \cos 2t + C_2 \sin 2t$   
 C)  $C_1 \cos t + C_2 \sin t$                       D)  $C_1 \cos 2t - C_2 \sin 2t$
- iv) In  $P_0(x)y'' + P_1(x)y' + P_2(x)y = 0$ , if  $P_0(x) = 0$ , then it has  
 A) Singular                      B) Regular singularity                      C) Exact                      D) Homogeneous
- b. Solve  $(D^2 - 3D + 2)y = \frac{1}{1+e^{-x}}$  using variation of parameters. (05 Marks)
- c. Solve  $x^2 y'' - x \frac{dy}{dx} + y = \log x$ . (05 Marks)
- d. Solve  $xy'' + y' + xy = 0$  using Frobenius series solution method. (06 Marks)

- 4 a. Choose the correct answers for the following : (04 Marks)
- i) The partial differential equation of the relation  $z = ax + a^2 y^2 + b$  is  $q = \underline{\hspace{2cm}}$ .  
 A)  $p^2 y$                       B)  $2p^2 y$                       C)  $p^2 y^2$                       D)  $2py^2$
- ii) The solution of  $\frac{\partial^2 z}{\partial x^2} = z$  is  $z = \underline{\hspace{2cm}}$ .  
 A)  $C_1(x)e^y + C_2(x)e^{-y}$                       B)  $C_1(x)e^y - C_2(x)e^{-y}$   
 C)  $C_1(y)e^x + C_2(y)e^{-x}$                       D)  $C_1(y)e^x - C_2(y)e^{-x}$
- iii) The solution of  $yq - xp = z$  by Lagrange's method is  $\underline{\hspace{2cm}} = 0$ .  
 A)  $f\left(\frac{x}{y}, \frac{y}{z}\right)$       B)  $f\left(\frac{y}{x}, \frac{y}{z}\right)$                       C)  $f\left(xyz, \frac{y}{z}\right)$                       D)  $f\left(xy, \frac{y}{z}\right)$ .
- iv) The solution of  $\frac{\partial u}{\partial x} = \frac{\partial u}{\partial y}$  by separation of variables with K as the common solution is  
 $u = \underline{\hspace{2cm}}$ .  
 A)  $Ce^{K(x+y)}$                       B)  $Ce^{Kxy}$                       C)  $Ce^{K(x+y)}$                       D)  $Ce^y$
- b. Form the partial differential equation from the relation  $f(x+y+z, x^2+y^2+z^2) = 0$ . (05 Marks)
- c. Solve  $y^2 p - xyq = x(z-2y)$  using Lagrange's linear form. (05 Marks)
- d. Solve  $x \frac{\partial z}{\partial x} - y \frac{\partial z}{\partial y} = 0$  using separation of variables. (06 Marks)

**PART - B**

- 5 a. Choose the correct answers for the following : (04 Marks)
- i) The value of  $\int_0^1 \int_0^6 xy dx dy$  is  $\underline{\hspace{2cm}}$ .  
 A) 6                      B) 7                      C) 8                      D) 9
- ii) Area of the ellipse by double integration is  $= \underline{\hspace{2cm}}$ .  
 A)  $\pi(a+b)$                       B)  $\pi(a-b)$                       C)  $\pi ab$                       D)  $\pi(b-a)$





iii) The value of  $\beta\left(\frac{1}{2}, \frac{1}{2}\right) = \underline{\hspace{2cm}}$ .

A)  $\sqrt{\pi}$

B)  $\pi$

D)  $\frac{\pi}{2}$

iv) The value of  $\Gamma\left(\frac{1}{4}\right) \times \Gamma\left(\frac{3}{4}\right) = \underline{\hspace{2cm}}$

A)  $\pi\sqrt{2}$

B)  $2\sqrt{\pi}$

D)  $2\pi$



b. Change the order of integration in,  $I = \int_0^1 \int_{x^2}^{2-x} xydydx$  and hence evaluate. (05 Marks)

c. Evaluate  $\int_1^e \int_1^{e^x} \int_1^{e^{xy}} \log z dz dx dy$ . (05 Marks)

d. Define Beta and Gamma functions, derive the relation as  $\beta(m, n) = \frac{\Gamma(m)\Gamma(n)}{\Gamma(m+n)}$ . (06 Marks)

6 a. Choose the correct answers for the following : (04 Marks)

i) If  $\int_C \vec{F} \cdot d\vec{r} = 0$  then F is called,

A) Singular

B) Irrotational

C) Solenoidal

D) Domain

ii) In Green's theorem  $\iint_S \left( \frac{\partial F_2}{\partial x} - \frac{\partial F_1}{\partial y} \right) dx dy = \underline{\hspace{2cm}}$ .

A)  $F_1 + F_2$ B)  $\int_C (F_1 dx + F_2 dy)$ C)  $\int_S F_1 dx + F_2 dy$ D)  $\int_C (F_1 dx + F_1 dy)$ 

iii) In Stoke's theorem  $\int_C \vec{F} \cdot d\vec{R} = \underline{\hspace{2cm}}$ .

A)  $\int_C \text{curl} \vec{F} \cdot \vec{N} ds$ B)  $\int_C \text{div} \vec{F} \cdot \vec{N} ds$ C)  $\int_C \text{grad} \vec{F} \cdot \vec{N} ds$ D)  $\int_S \text{curl} \vec{F} \cdot \vec{N} ds$ 

iv) If  $\vec{F} = x^3 \vec{i} + y^3 \vec{j} + z^3 \vec{k}$  then  $\text{div} \vec{F} = \underline{\hspace{2cm}}$

A)  $x^2 + y^2 + z^2$ B)  $2(x^2 + y^2 + z^2)$ C)  $3(x^2 + y^2 + z^2)$ D)  $3(x^2 \vec{i} + y^2 \vec{j} + z^2 \vec{k})$ 

b. If  $\vec{F} = (3x^2 + 6y)\vec{i} - 14yz\vec{j} + 20xz^2\vec{k}$ , evaluate  $\int_C \vec{F} \cdot d\vec{r}$  from (0, 0, 0) to (1, 1, 1) along the curve given by  $x = t, y = t^2, z = t^3$ . (05 Marks)

c. Use Green's theorem to evaluate  $\int_C (y - \sin x) dx + \cos x dy$ , where C is the triangle in

xy-plane bounded by the lines  $y = 0, x = \frac{\pi}{2}$  and  $y = \frac{2x}{\pi}$ . (05 Marks)

d. Use Gauss divergence theorem to evaluate  $\int_S \vec{F} \cdot \vec{N} ds$  where  $\vec{F} = 4xy\vec{i} + yz\vec{j} - xz\vec{k}$  and S is the surface of the cube bounded by the planes  $x = 0, x = 2, y = 0, y = 2, z = 0, z = 2$ . (06 Marks)

7 a. Choose the correct answers for the following : (04 Marks)

i)  $L\{e^{-t} \cosh t\} = \underline{\hspace{2cm}}$

A)  $\frac{s+1}{(s-1)^2 + 1}$

B)  $\frac{s-1}{(s+1)^2 + 1}$

C)  $\frac{s+1}{(s-1)^2 - 1}$

D) None of these



ii)  $L\{t^{-1}f(t)\} = \underline{\hspace{2cm}}$

- A)  $\int_s^\infty F(s)ds$       B)  $\int_s^\infty f(t)dt$       C)  $\int_t^\infty F(s)ds$       D)  $\int_0^\infty f(t)dt$

iii) When T denotes period of the function  $f(t)$  then,  $\frac{1}{1-e^{-ST}} \int_0^T e^{-st}f(t)dt = \underline{\hspace{2cm}}$ .

- A)  $f(t) + C$       B)  $L\{f(t)e^{-st}\}$       C)  $L\{f(t)\}$       D)  $L\{e^t\}$

iv) In unit step function if  $u(t-a) = 0$  then,

- A)  $t < a$       B)  $t \geq a$       C)  $t = a$       D)  $t \leq a$

b. Find the Laplace transform of the function  $f(t) = te^{-t} \sin^2 3t$ . (05 Marks)

c. Find the Laplace transform of the function,

$$f(t) = \begin{cases} t, & \text{for } 0 < t \leq a \\ 2a - t, & \text{for } a < t < 2a \end{cases}, 2a \text{ is the period.} \quad (05 \text{ Marks})$$

d. Express  $f(t)$  in terms of unit step function and find the Laplace transform when,

$$f(t) = \begin{cases} t^2, & 0 < t < 2 \\ 4t, & 2 < t < 4 \\ 8, & t > 4 \end{cases} \quad (06 \text{ Marks})$$

8 a. Choose the correct answers for the following : (04 Marks)

i) The value of  $L^{-1}\left\{\frac{s^2 - 3s + 4}{s^3}\right\} = \underline{\hspace{2cm}}$ .

- A)  $1 - 3t^2 + 2t$       B)  $\frac{1+3t}{2t^2}$       C)  $1 - 3t + 2t^2$       D)  $\frac{1+2t^2}{3t}$

ii) The value of  $L^{-1}\left\{\frac{s}{(s-2)^2}\right\} = \underline{\hspace{2cm}}$

- A)  $e^{2t}(1-2t)$       B)  $e^{2t}(1+2t)$       C)  $e^{2t}(2+2t)$       D)  $2+2t$

iii) By convolution theorem  $L^{-1}\left\{\frac{1}{(s+1)(s+2)}\right\} = \underline{\hspace{2cm}}$ .

- A)  $\int_0^\infty e^{-t}e^{t-2}dt$       B)  $\int_0^t e^{-t}e^{-(t-2)}dt$       C)  $\int_0^t e^{-u}e^{-(t-u)(2)}du$       D)  $\int_0^\infty e^{-2t}e^{t^2+1}dt$

iv) Laplace transform of  $\frac{dy}{dt} + y = 0$  with  $y(0) = 1$  is =  $\underline{\hspace{2cm}}$

- A)  $e^{-t}$       B)  $e^t$       C)  $te^t$       D)  $\frac{e^t}{t}$

b. Find the inverse Laplace transform of,  $F(s) = \frac{2s^2 - 6s + 5}{s^3 - 6s^2 + 11s - 6}$ . (05 Marks)c. Find  $L^{-1}\left\{\frac{s}{(s-1)(s^2+4)}\right\}$  by convolution theorem. (05 Marks)d. Solve by Laplace transform method,  $\frac{d^2y}{dt^2} - 3\frac{dy}{dt} + 2y = 4t + 12e^{-t}$  with  $y(0) = 6$ ,  $y'(0) = -1$ 

(06 Marks)

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