



Second Semester B.E. Degree Examination, Dec.2018/Jan.2019
Engineering Mathematics - II

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing at least two from each part.

PART - A

- 1 a. Choose the correct answers for the following : (04 Marks)
- The solution of the first order equation, $P^2 - 5P - 14 = 0$ is,
 A) $(y - 7x - c)(y - 2x - c) = 0$ B) $(y - 7x - c) = 0$
 C) $(x + y - c) = 0$ D) $(y - 2x - c) = 0$
 - The solution of the equation $P = \log(px - y)$ is,
 A) $y = cx + \sin^{-1} c$ B) $y = cx - e^c$ C) $y = cx + e^c$ D) $y = cx - \sin^{-1} c$
 - If $\frac{dx}{dp} + \frac{2}{p}x = 2$ be the linear differential equation then the integrating factor is,
 A) $\frac{1}{p^2}$ B) p^2 C) $-p^2$ D) $\log p$
 - The differential equation of atmospheric pressure at any height Z is,
 A) $\frac{dP}{dZ} = \frac{-\rho g}{K}$ B) $\rho = \frac{P}{K}$ C) $P = \frac{\rho}{K}$ D) $P = \rho K$
- b. Solve : $xy\left(\frac{dy}{dx}\right)^2 + \frac{dy}{dx}(3x^2 - 2y^2) = 6xy$ (04 Marks)
- c. Solve : $y = 2Px + P^m$ (06 Marks)
- d. Solve : $e^{3x}(P-1) + P^3e^{3y} = 0$ (06 Marks)
- 2 a. Choose the correct answers for the following : (04 Marks)
- A general solution of a linear differential equation of 3rd order contains,
 A) One constant B) Two constants C) Three-constants D) n-constants
 - The solution of the differential equation, $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} = 0$ is,
 A) $y = C_1e^{-x} + C_2e^{2x}$ B) $y = C_1 + C_2e^{2x}$ C) $y = (C_1 + C_2x)e^{2x}$ D) $C_1x = C_2$
 - Particular integral of the differential equation $\frac{d^2y}{dx^2} + y = \cos 2x$ is,
 A) $\frac{1}{5}\sin 2x$ B) $-\frac{1}{3}\cos 2x$ C) $\frac{1}{3}\cos 2x$ D) $\frac{1}{3}\sin 2x$
 - Particular integral of the differential equation, $y'' + 2y = 2$ is,
 A) 1 B) 2 C) 3 D) None of these
- b. Solve : $e^x \frac{d^2y}{dx^2} + 2e^x \frac{dy}{dx} + e^x y = x^2$ (04 Marks)
- c. Solve the initial value problem, $\frac{d^2y}{dx^2} + 4\frac{dy}{dx} + 5y + 2\cosh x = 0$, given $y = 0$, $\frac{dy}{dx} = 1$ at $x = 0$. (06 Marks)
- d. Solve : $\frac{dx}{dt} + 4x + 3y = t$; $\frac{dy}{dt} + 2x + 5y = e^t$ (06 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
 2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice.



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(04 Marks)

- 3 a. Choose the correct answers for the following : (04 Marks)
- The Wronskian of $u = xe^x$ and $v = e^x$ is,
A) xe^x B) x^2e^x C) $-e^{2x}$ D) $xe^x + e^x$
 - A linear differential equation in which there are 2 or more dependent variables and single independent variable is known as,
A) Exact equation B) Bernoulli's equation
C) Simultaneous equation D) Cauchy's linear equation
 - Cauchy's differential equation is a special case of Legendre's linear equation is,
A) $a = 1 = b$ B) $a = 0, b \neq 1$ C) $a = 1, b = 0$ D) $a = 0 = b$
 - In Frobenius method, equating to zero the coefficient of the lower degree in x gives a quadratic equation known as,
A) Frobenius equation B) Indicial equation
C) Linear equation D) Multiple equation
- b. Solve by the method of variation parameter, $y'' + 2y' + 2y = e^{-x} \sec^3 x$ (05 Marks)
- c. Solve : $x^2 \frac{d^2y}{dx^2} - x \frac{dy}{dx} + y = x^2$ (05 Marks)
- d. Obtain the series solution of the equation, $9x(1-x) \frac{d^2y}{dx^2} - 12 \frac{dy}{dx} + 4y = 0$ (06 Marks)
- 4 a. Choose the correct answers for the following : (04 Marks)
- The partial differential equation of $z = f(x^2 + y^2)$ is,
A) $yp - xq = 0$ B) $p^2 + q^2 = 0$ C) $z = p^2q^2$ D) None of these
 - The solution of the equation $\frac{\partial^2 z}{\partial x^2} = xy$ is,
A) $\frac{x^3 y^3}{6}$ B) $\frac{y^3 x}{6}$ C) $\frac{x^3 y}{6} + xf(y) + \phi(y)$ D) $x^2 + y^2 + y$
 - The solution of partial differential equation $\sqrt{p} + \sqrt{q} = 2$ is,
A) $ax + (2 - \sqrt{a})^2 y + c$ B) $\frac{y}{x}$ C) $\frac{ay}{bx}$ D) $ay - (2 - \sqrt{a})^2 x + c$
 - The partial differential equation of the form $z = px + qy + f(pq)$ in two variables is known as,
A) Clairaut's form B) Lagrange's form C) Bessel's form D) Legendre's form
- b. Solve : $\phi(x + y + z, x^2 + y^2 + z^2) = 0$ (04 Marks)
- c. Solve : $(x^2 - y^2 - z^2)p + 2xyq = 2xz$ (06 Marks)
- d. Solve by the method of separation of variables. $4 \frac{\partial u}{\partial x} + \frac{\partial u}{\partial y} = 3u$ (06 Marks)

PART - B

- 5 a. Choose the correct answers for the following : (04 Marks)
- While computing the volume for $f(x, y, z)$, which of the following expression is true
A) $\iiint_R dx dy dz = \int_v dv$ B) $\iiint_R dr d\theta dz = \int_v dv$
C) $\iiint_R r \sin \theta dr d\theta d\phi = \int_v dv$ D) None of these
 - The value of $\int_0^1 \int_0^1 xy dx dy$ is,
A) 0 B) $\frac{1}{4}$ C) $\frac{1}{2}$ D) 1



- iii) The value of $\sqrt{\frac{1}{4}} \cdot \sqrt{\frac{3}{4}}$ is,
- A) $\sqrt{\pi}$ B) $\sqrt{2\pi}$ C) $2\sqrt{\pi}$ D) 2π
- iv) The function $\beta(m, n)$ is not equal is,
- A) $\frac{\Gamma(n)\Gamma(m)}{\Gamma(n+m)}$
B) $B\frac{(m+1, n)}{m} \times (m+n)$
C) $\frac{B(m, m+1)}{n}$
D) $B(n, m)$
- b. Evaluate $\iint_A xy dx dy$ where A is the region bounded by the x-axis ordinate $x = 2a$ and the parabola $x^2 = 4ay$. (06 Marks)
- c. Evaluate $\iiint_R (x+y+z) dx dy dz$ where R is the tetrahedron, $x = 0, y = 0, z = 0$ and $x + y + z = 1$. (06 Marks)
- d. Prove that $\int_0^\infty e^{-x^2} dx = \frac{\sqrt{\pi}}{2}$. (04 Marks)
6. a. Choose the correct answers for the following: (04 Marks)
- i) For any closed surface S the value of $\iint_S \text{Curl } \vec{F} \cdot \vec{N} ds =$ _____
- A) 1 B) 0 C) $\frac{2}{3}$ D) $\frac{1}{3}$
- ii) Two vectors \vec{a} and \vec{b} are perpendicular if,
- A) $\vec{a} \cdot \vec{b} = 1$ B) $\vec{a} \times \vec{b} = 0$
C) $\cos \theta = 0$, where θ is angle between \vec{a} and \vec{b} D) None of these
- iii) Vector \vec{F} is irrotational if,
- A) $\text{Curl } \vec{F} = 0$ B) $\text{Div } \vec{F} = 0$ C) $\text{Curldiv } \vec{F} = 0$ D) None of these
- iv) If \vec{F} is a continuously differential vector function in the region E bounded by the closed surface S then Gauss divergence theorem is,
- A) $\int_S \vec{F} \cdot \vec{N} ds = \int_E \text{div } \vec{F} dV$
B) $\int_S \vec{F} \cdot \vec{N} ds = \int_E \text{Curl } \vec{F} dV$
C) $\int_S \vec{F} \cdot \vec{N} ds = \int_E \nabla \phi dV$
D) $\int_S \vec{F} \cdot \vec{N} ds = \int_E \nabla \cdot \nabla \vec{F} dV$
- b. If $\vec{F} = 3xyi - y^2j$ evaluate $\int_C \vec{F} \cdot d\vec{R}$ where C is the arc of the parabola $y = 2x^2$ from $(0, 0)$ to $(1, 2)$. (04 Marks)
- c. Verify Green's Theorem for $\int_C [(xy + y^2)dx + x^2dy]$ where C is bounded by $y = x$ and $y = x^2$. (06 Marks)
- d. Evaluate $\oint_C \vec{F} \cdot d\vec{R}$ Stoke's theorem where $\vec{F} = y^2i + x^2j - (x+z)k$ and C is the boundary of the triangle with vertices at $(0, 0, 0), (1, 0, 0)$ and $(1, 1, 0)$ (06 Marks)



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(04 Marks)

- 7 a. Choose the correct answers for the following :

i) If $L[f(t)] = F(s)$ then $L[f(at)]$ is equal to

A) $F(sa)$ B) $aF\left(\frac{s}{a}\right)$ C) $\frac{1}{a}F(as)$ D) $\frac{1}{a}F\left(\frac{s}{a}\right)$

ii) $L\left[\frac{1-e^{-at}}{t}\right] =$

A) $\log\left(1+\frac{a}{s}\right)$ B) $\log\left(\frac{a}{s}\right)$ C) $\log\left(1-\frac{a}{s}\right)$ D) $\log\left(\frac{s}{a}\right)$

iii) Laplace transform of $t \sin 2t$ is,

A) $\frac{2}{(s^2 + a^2)^2}$ B) $\frac{4s}{(s^2 + 4)^2}$ C) $\frac{s}{(s^2 + 4)^2}$ D) $\frac{s}{(s^2 - a^2)^2}$

iv) Laplace transform of $e^{at}\delta(t-b)$ is equal to

A) $e^{-(s-a)b}$ B) $e^{(s-a)b}$ C) $e^{-(s+a)b}$ D) None of these

b. Prove that $L[t^n f(t)] = (-1)^n \frac{d^n F(s)}{ds^n}$

(04 Marks)

c. Find the Laplace transform of the triangular wave function of period $2a$ given by,

$$f(t) = \begin{cases} t & 0 < t < a \\ 2a-t & a < t < 2a \end{cases} \quad (06 \text{ Marks})$$

d. Express the function in terms of Heaviside's unit step function and find its Laplace

$$\text{transform, } f(t) = \begin{cases} \sin t & 0 \leq t \leq \pi \\ t & \pi \leq t \leq 2\pi \\ \cos t & t > 2\pi \end{cases} \quad (06 \text{ Marks})$$

- 8 a. Choose the correct answers for the following :

(04 Marks)

i) Inverse Laplace transform of $\frac{s^3 + s^2 + 6}{s^4}$ is,

A) $1+t+t^2$ B) $2+3t+4t^4$ C) $t+t^2+3t^3$ D) $\frac{1+t^3}{t}$

ii) Inverse Laplace transform of $F(s-a)$ is,

A) $e^{at}L^{-1}[f(t)]$ B) $e^{-at}[f(t)]$ C) $L^{-1}[e^{-at}F(s)]$ D) None of these

iii) The differential equation, $y'' + 2y' + 5y = 8\sin t + 4\cos t$ under the conditions $y(0) = 1$,

$y\left(\frac{\pi}{4}\right) = \sqrt{2}$ is an,

A) Initial value problem

B) Boundary value problem

C) Both (A) and (B)

D) None of these

iv) Inverse Laplace transform of $\frac{F(s)}{s}$ is,

A) $\int_0^\infty f(u)du$ B) $\int_0^t f(u)du$ C) $\int_0^t \frac{F(u)}{u} du$ D) $\int_0^\infty e^{-st} dt$

b. Find the inverse Laplace transform of, $\frac{2s^2 - 6s + 5}{s^3 - 6s^2 + 11s - 6}$.

(04 Marks)

c. Evaluate using convolution theorem, $L^{-1}\left[\frac{1}{s^2(s^2 + 16)}\right]$.

(06 Marks)

d. Solve $y'' + 6y' + 9y = 12t^2 e^{-3t}$ given $y(0) = y'(0) = 0$ by Laplace transform method. (06 Marks)

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