



15EC43

Fourth Semester B.E. Degree Examination, June/July 2018 Control Systems

Time: 3 hrs.

USN

Max. Marks: 80

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

a. Write the differential equations for the mechanical system shown in Fig.Q1(a) and obtain F-V analogy. (06 Marks)

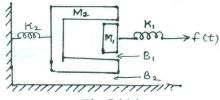
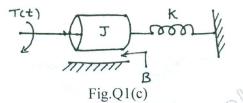


Fig.Q1(a)

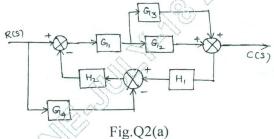
- b. Differentiate between open loop control system and closed-loop control system. (06 Marks)
- For the rotational system shown in Fig.Q1(c). Draw torque-voltage analogous circuit

(04 Marks)



OR

a. Reduce the following block diagram of the system shown on Fig.Q2(a) into a single equivalent block diagram by block diagram reduction rules. (06 Marks)



b. Find $\frac{C(s)}{R(s)}$ for the following signal flow graph. [Refer Fig.Q2(b)]

(06 Marks)

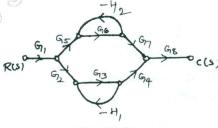
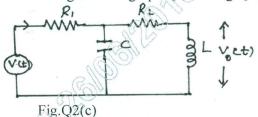


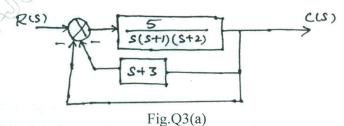
Fig.Q2(b)

- c. For the following circuit write the signal flow graph. [Refer Fig.Q2(c)]
- (04 Marks)



Module-2

3 a. For the system shown in Fig.Q3(a). Find the : i) system type ii) static error constants k_p , k_v and k_a and iii) the steady state error for an input r(t) = 3 + 2t. (06 Marks)



- Find the step-response, C(t) for the system described by $\frac{C(s)}{R(s)} = \frac{4}{S+4}$. Also find the time
 - constant, rise time and settling time.

(05 Marks)

c. Derive the equation for steady state error of simple closed loop system.

(05 Marks)

OR

4 a. A second order system is represented by the transfer function.

$$\frac{Q(s)}{I(s)} = \frac{1}{JS^2 + fS + K}$$

A step input of 10 Nm is applied to the system and the test results are:

- i) maximum overshoot = 6%
- ii) time at peak overshoot = 1sec
- iii) the steady state value of the output is 0.5 radian.

Determine the values of J, f and K.

(06 Marks)

- b. A system has 30% overshoot and settling time of 5 seconds for on unit step input.

 Determine: i) The transfer function ii) peak time 't_p' iii) output response (assume e_{ss} as 2%).

 (06 Marks)
- c. Write the general block diagrams of the following:
 - i) PD type of controller
 - ii) PI type of controller.

(04 Marks)

Module-3

5 a. Determine the ranges of 'K' such that the characteristic equation:

 $S^3 + 3(K+1)S^2 + (7K+5)S + (4K+7) = 0$ has roots more negative than S = -1. (06 Marks)

b. Check the stability of the given characteristic equation using Routh's method.

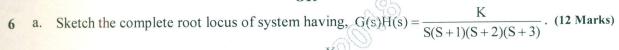
$$S^6 + 2S^5 + 8S^4 + 12S^3 + 20S^2 + 16S + 16 = 0.$$

(06 Marks)

c. Mention few limitations of Routh's criterion.

(04 Marks)

OR



b. Consider the system with $G(S)H(s) = \frac{1}{S(S+1)(S+4)}$. Find whether S = -2 point is on root locus or not using angle condition. (04 Marks)

Module-4

- 7 a. The open loop transfer function of a system is $G(s) = \frac{K}{s(1+s)(1+0.1s)}$. Determine the values of K such that i) gain margin = 10 dB ii) phase margin = 24°. Use Bode plot. (10 Marks)
 - b. Derive the expression for resonant peak 'M_r' and corresponding resonant frequency 'W_r' for a second-order underdamped system in frequency response analysis. (06 Marks)

OR

8 a. Sketch the Nyquist plot for a system with the open-loop transfer function:

G(s)H(s) =
$$\frac{k(1+0.5s)(1+s)}{(1+10s)(s-1)}$$

Determine the range of values of 'k' for which the system is stable. (08 Marks)

b. Write the polar plot for the following open-loop transfer function:

$$G(S)H(s) = \frac{1}{1+0.1s}$$
.

c. Explain Nyquist stability criteria.

(04 Marks)

Module-5

9 a. Explain spectrum analysis of sampling process.

(06 Marks)

b. Explain how zero-order hold is used for signal reconstruction.

(04 Marks)

c. Find the state–transition matrix for $A = \begin{bmatrix} 0 & -1 \\ +2 & -3 \end{bmatrix}$. (06 Marks)

OR

a. Obtain an appropriate state model for a system represented by an electric circuit as shown in Fig.Q10(a).

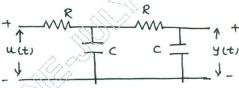


Fig.Q10(a)

(06 Marks)

b. A linear time invariant system is characterized by the homogeneous state equation :

$$\begin{bmatrix} \bullet \\ \mathbf{x}_1 \\ \bullet \\ \mathbf{x}_2 \end{bmatrix} = \begin{bmatrix} 1 & 0 \\ 1 & 1 \end{bmatrix} \begin{bmatrix} \mathbf{x}_1 \\ \mathbf{x}_2 \end{bmatrix}$$

Compute the solution of homogeneous equation, assume the initial state vector.

$$X_0 = \begin{bmatrix} 1 \\ 0 \end{bmatrix}$$
 (06 Marks)

c. State the properties of state transition matrix. (04 Marks)