

USN

17EC36

Third Semester B.E. Degree Examination, June/July 2019 Engineering Electromagnetics

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

1 a. State and explain Coulomb's law of force between two point charges in vector form.

Identical point charges of 3µC are located at four corners of the square of 5 cm side. Find the magnitude of the force on any charge.

(08 Marks)

c. Define Electric Field Intensity. Derive the electric field intensity due to 'n' number of point charges.

(06 Marks)

OR

2 a. Derive the expression for the electric field intensity due to infinite line charge. (06 Marks)

b. Obtain the expression for an electric field intensity due to charged circular ring of radius 'r' placed in x-y plane, at a point (0, 0, z), having uniform line charge density of ρ_L (c/m).

(06 Marks)

(06 Marks)

c. A uniform line charge $\rho_L = 25$ nc/m lies on the line x = -3m and y = 4m in free space. Find the electric field intensity at a point (2, 3, 15) (06 Marks)

Module-2

a. State and explain Gauss's law and prove Gauss's law as applied to point charge. (06 Marks)

b. Given that the field $\vec{D} = \frac{5\sin\theta\cos\phi}{r}$ ar (c/m^2) . Find volume charge density. (06 Marks)

c. Given D = 5r ar (c/m^2) , prove divergence theorem for a shell region enclosed by spherical surfaces at r = a and r = b (b > a) and centered at the origin. (08 Marks)

OR

4 a. Explain the concept of work and potential and obtain the expression for potential difference between two points due to an electric field produced by a point charge. (06 Marks)

b. Obtain the point form of continuity equation.

c. Given the current density $\vec{J} = \frac{2}{r^2} \cos\theta \, \vec{ar} + 20e^{-2r} \sin\theta \, \vec{a\theta} - r\sin\theta \cos\phi \, \vec{a\phi}$ (A/m²)

i) Find J at r = 3m, $\theta = 0^{\circ}$, $\phi = \pi$.

ii) Find the total current passing through spherical surface r = 3m, $0 < \theta < 20^{\circ}$, $0 < \phi < 2\pi$.

(08 Marks)

Module-3

5 a. From point form of Gauss's law, derive Poisson's and Laplace's equation. (05 Marks)

b. State and prove uniqueness theorem.

(08 Marks)

(06 Marks)

c. Applying Laplace's equation, obtain the expression for capacitance of a parallel plate capacitor. The distance between two plates are 'd' and the area of plate is 'A'. (07 Marks)

2. Any revealing of identification, appeal to evaluator and /or equations written eg, 42+8 = 50, will be treated as malpractice. Important Note: 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.



OR

- 6 a. Using Biot Savart law obtain the expression for magnetic field intensity at a point due to infinitely long straight conductor. (08 Marks)
 - b. Given the magnetic field $\overrightarrow{H} = 2r^2(z+1)\sin\phi$ a $\overrightarrow{\phi}$. Verify stokes theorem for the portion of a cylindrical surface defined by r=2, $\frac{\pi}{4} \le \phi \le \frac{\pi}{2}$, $1 \le z \le 1.5$ and for its perimeter. Given vector magnetic potential. (08 Marks)
 - c. $\vec{A} = x^2 \vec{a}_x + 2yz \vec{a}_y x^2 \vec{a}_z$. Find the magnetic flux density.

(04 Marks)

Module-4

- 7 a. Derive the expression for the force acting on a differential current element placed in a magnetic field. (06 Marks)
 - b. A point charge Q = -1.2 (C) has velocity $\vec{V} = 5\vec{a}_x + 2\vec{a}_y 3\vec{a}_z$ m/s. Find the magnitude of the force exerted on the charge if
 - i) $\vec{E} = -18\vec{a}_x + 5\vec{a}_y 10\vec{a}_z \text{ (V/m)}$
 - ii) $\vec{B} = -4\vec{a}_x + 4\vec{a}_y + 3\vec{a}_z$ (T)

(06 Marks)

c. A current element $I_1 dL_1 = 10^{-4} \vec{a_z}$ (A.m) is located at $P_1(2, 0, 0)$ and another current element $I_2 dL_2 = 10^{-6} (\vec{a_x} - 2\vec{a_y} + 3\vec{a_z})$ (A.m) is located at $P_2(-2, 0, 0)$. Find the force exerted on $I_1 dL_1$ by $I_2 dL_2$.

OR

- 8 a. Discuss the magnetic boundary conditions as applicable to B and H at the interface between two different magnetic materials. (10 Marks)
 - b. Write short notes on:
 - i) Energy Density in magnetic field ii) Forces on magnetic materials. (10 Marks)

Module-5

- 9 a List Maxwell's equations in integral form and derive the point form of Maxwell's equation for time varying fields. (12 Marks)
 - b. Show that in a capacitor the conduction current density is equal to displacement current density for applied voltage V(t) = V₀ Cos wt. (08 Marks)

OF

- 10 a What is Uniform plane wave? Derive the expression of uniform plane wave travelling in free space.

 (10 Marks)
 - b. State and prove Poynting theorem. Also show that average power

$$P_{avg} = \frac{1}{2} \frac{E_m^2}{\eta} (W/m^2).$$
 (10 Marks)

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