



USN	

10ES36

Third Semester B.E. Degree Examination, Dec.2017/Jan.2018 Field Theory

Time: 3 hrs.

Max. Marks: 100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

PART - A

1 a. State and prove gauss law for electrostatics.

(06 Marks)

- b. If $E = \left(-8xy\hat{a}_x 4x^2\hat{a}_y + \hat{a}_z\right)$ V/mt. Find the work done in carrying a 6 C charge from A(1, 8, 5) to B(2, 18, 6) along the path y = 3x + 2 x + 4 (06 Marks)
- c. Four point charges each 20 us are at A(4, 0, 0), B(-4,0,0), C(0,4,0), D(0,-4,0) respectively. Find the force on a 200 µC point charge at (0, 0, 3). (08 Marks)
- a. Derive an equation for divergence of flux density in differential form, and hence explain Gauss divergence theorem. (08 Marks)
 - b. A 15 nC point charge is at the origin in free space. Calculate v_1 if point P is located at (2, -3, -1). Also calculate v_1 at P if v = 0 at (6, 5, 4) (06 Marks)
 - c. Deduce an expression for energy and energy density in an electro static field. (06 Marks)
- 3 a. Using Poisson's equation, obtain the expression for junction potential in a p-n junction.

(08 Marks)

- b. Derive Laplace's equation and hence write the expression for Laplacian of V in cylindrical and spherical co-ordinates. (06 Marks)
- c. Find E at P(3, 1, 2) for the field of two co-axial conducting cylinders. V = 50 V at r = 2 m, V = 20 V at r = 3 m.
- 4 a. Derive an expression for magnetic flux density (B) due to straight conductor of finite length. (06 Marks)
 - b. If H in a region is $2x\hat{a}_y + (3y 2)\hat{a}_z$, find the current density at the origin (06 Marks)
 - c. Given the magnetic field $H = 2r^2(z+1)\sin\phi\hat{a}_{\phi}$, verify Stoke's theorem for the portion of cylindrical surface defined by r = 2, $\frac{\pi}{4} < \phi < \frac{\pi}{2}$, 1 < z < 1.5.

PART - B

- 5 a. Find the magnetic flux density due to long current carrying conductor using vector magnetic potential. (08 Marks)
 - b. Derive the expression for boundary conditions, if the field lines are tangent and normal to the boundary line between two media's in static magnetic field. (06 Marks)
 - c. A solenoid with air core has 2000 turns and a length of 500 mm, core radius 40 mm. Find its inductance. (06 Marks)

6 a. Derive the modification of Ampere's circuit law to suit for time varying conditions.

(06 Marks)

- b. Explain Maxwell's equations in point and integral form. Establish relationship between conduction current density and displacement current density for the given field $E = E_0 \sin \omega t$ (08 Marks)
- c. Do the fields $E = E_m \sin x \sin t \hat{a}_y$ and $\vec{H} = \frac{E_m}{\mu} \cos x \cos t \hat{a}_z$. Satisfy Maxwell's equations. Verify. (06 Marks)
- 7 a. Derive an expression for electric and magnetic wave equations

(06 Marks)

- b. For an electromagnetic wave propagating in free space, show that $\frac{E}{H} = \eta$. (08 Marks)
- c. Find skin depth and surface resistance of copper conductor at 100 MHz having conductivity $\sigma = 5.8 \times 10^7 \,\text{T/m}$ and $\mu = 100$. (06 Marks)
- 8 a. Explain the reflection of uniform plane wave with normal incidence at a plane dielectric boundary. (10 Marks)
 - b. Write short notes on:
 - (i) Reflection co-efficient.
 - (ii) Standing wave ratio.

(10 Marks)