

## Fifth Semester B.E. Degree Examination, Dec.2015/Jan.2016 Formal Languages & Automata Theory

angalore

Time: 3 hrs.

Max. Marks: 100

Note: Answer FIVE full questions, selecting at least TWO questions from each part.

PART - A

What is Automata? Discuss why study automata.

(06 Marks)

Mention the differences between DFA, NFA and NFA-€.

(04 Marks)

Design a DFA to accept the language  $L = \{W \mid W \text{ is of even length and begins with } 01\}$ .

- d. Design the NFA-∈ or NFA for the languages given below:
  - i) abc, abd and aacd {Assume  $\sum = a, b, c, d$ }
  - ii) {ab, abc}\* {Assume  $\sum = a, b, c$ }

(04 Marks)

Covert the following NFA-∈ to DFA using "Subset construction scheme".

(08 Marks)

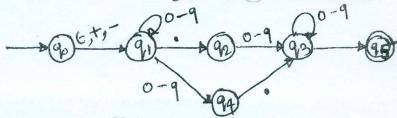


Fig. Q2 (a)

b. Define Regular expression and write regular expression for the following languages:

i)  $L = \{a^{2n}b^{2m} : n \ge 0, m \ge 0\}$ 

ii) Language over {0, 1} having all strings not containing 00.

(06 Marks)

c. Convert the regular expression  $(0+1)^*1(0+1)$  to a NFA- $\in$ .

(06 Marks)

State and prove pumping Lemma theorem for regular languages. 3 Show that  $L = \{a^n b^n \mid n \ge 0\}$  is not regular. (08 Marks)

b. What is Homomorphism? Explain with an example.

(04 Marks)

Consider the transition table of DFA given below:

	0	1
$\rightarrow A$	В	A
В	A	C
C	D	В
*D	D	A
E	D	F
F	G	E
G	F	G
Н	G	D
Fig (3 (c)		

- Draw the table of distinguishabilities of states.
- ii) Construct the equivalent minimized DFA.

(08 Marks)

- 4 a. Obtain a grammar to generate integers and write derivation for the unsigned integer 1965.
  - b. Consider the grammar:

 $S \rightarrow aS \mid aSbS \mid \in$ 

Is the above grammar ambiguous? Show that the string aab has two -

- i) Parse trees
- ii) Left most derivations
- iii) Rightmost derivations

(12 Marks)

## PART - B

- 5 a. Define PDA. Design PDA to accept the language  $L(M) = \{\omega C\omega^R \mid \omega \in (a+b)^*\}$  by a final state and also give the graphical representation of PDA. (12 Marks)
  - b. Convert the following CFG to PDA:

 $S \rightarrow aABB \mid aAA$ 

 $A \rightarrow aBB \mid a$ 

 $B \rightarrow bBB \mid A$ 

 $C \rightarrow a$ 

(08 Marks)

**6** a. Consider the following grammar:

 $S \rightarrow ASB \in$ 

 $A \rightarrow aAS \mid a$ 

 $B \rightarrow SbS \mid A \mid bb$ 

- i) Are there any useless symbols? Eliminate if so.
- ii) Eliminate  $\in$  productions.
- iii) Eliminate unit productions.
- iv) Put the grammar into Chomsky Normal Form.

(08 Marks)

b. Show that  $L = \{a^n b^n c^n \mid n \ge 0\}$  is not context free.

(04 Marks)

c. Prove that the context free languages are closed under union, concatenation and reversal.

(08 Marks)

7 a. Design a turing machine that performs the following function:

 $q_0\omega \mid - *q_1\omega\omega$  for any  $\omega \in \{1\}*$ 

and also write its transition diagram.

(12 Marks)

- b. Explain the general structure of multitape and non deterministic turing machines. (08 Marks)
- **8** Write short notes on:
  - a. Applications of regular expressions.
  - b. Applications of context free Grammars.
  - c. Post's correspondence problem.
  - d. Chomsky hierarchy.

(20 Marks)

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