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Eighth Semester B.E. Degree Examination, June/July 2017 Finite Element Analysis

Time: 3 hrs.

Max. Marks: 100

Note: Answer any FIVE full questions, selecting at least TWO questions from each part.

PART - A

- 1 a. Indicate state of stress and strain at a point in terms of $\{\sigma\}$ and $\{\epsilon\}$. Mention its practical importance. (05 Marks)
 b. How potential energy functions are classified as stable/unstable/neutral? Give examples. (08 Marks)
 c. Obtain stiffness relation(K) with nodal force(F) and nodal displacement(Q) using energy principles. (07 Marks)

- 2 a. Mention the steps followed in Galenkin's method while finding displacement of a cantilever beam. (08 Marks)
 b. Using Rayleigh-Ritz method, derive an equation for maximum deflection for a simply supported beam at the center using Trigonometric function. (12 Marks)

- 3 a. What are displacement functions? Mention its types. Which one of them is widely used and why? (08 Marks)
 b. Obtain the expression of variation of shape functions for one dimensional bar element in terms of :
 i) L_1 and L_2 ii) x_1 and x_2 . (12 Marks)

- 4 a. Obtain the relation between nodal displacement of truss element in local and global coordinates. (04 Marks)
 b. Determine nodal displacements and forces for the truss (two bar) shown in Fig.4(b).

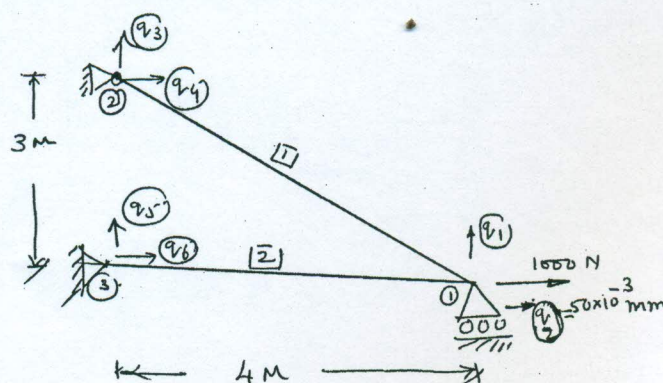


Fig.Q4(b)

Assume $q_2 = 50 \times 10^{-3}$ mm at node (i) roller support no nodal displacements at hinge support. (16 Marks)

Important Note : 1. On completing your answers, compulsorily draw diagonal cross lines on the remaining blank pages.
2. Any revealing of identification, appeal to evaluator and/or equations written eg. 42+8 = 50, will be treated as malpractice.

PART - B

- Obtain strain-displacement matrix for 4 noded 2 dimensional rectangular element assuming 2DOF at each node. Consider natural coordinates. (10 Marks)
- b. Obtain strain-displacement matrix and strains ϵ_x , ϵ_y and γ_{xy} for the element shown in Fig.Q5(b). Assume nodal displacements vector $\{q\} = \{2, 1, 1, -4, -3, 7\} \times 10^{-2}$ mm. (10 Marks)

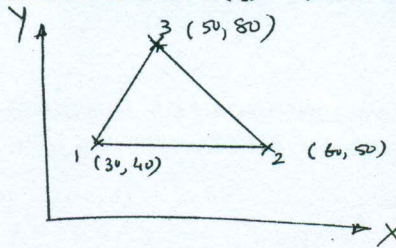


Fig.Q5(b)

- 6 Obtain shape functions for the following elements using Lagrange interpolation function and sketch the variation, shown in Fig.Q6. (20 Marks)

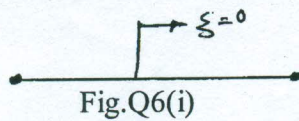


Fig.Q6(i)

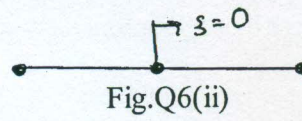


Fig.Q6(ii)

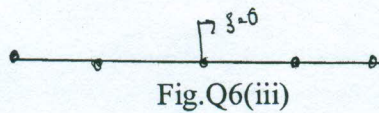


Fig.Q6(iii)

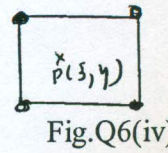


Fig.Q6(iv)

- 7 a. What are isoperimetric elements? Distinguish super from sub parametric elements with sketches. (08 Marks)
- b. Convert the following parent elements shown in Fig.Q7 to global Cartesian coordinate system having arbitrary curved/surfaces. No equations be derived. Only sketch the transformed shapes. (12 Marks)

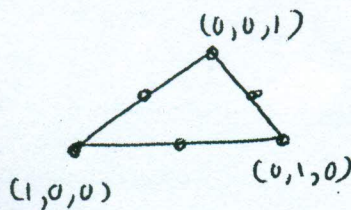


Fig. Q7(b)(i)

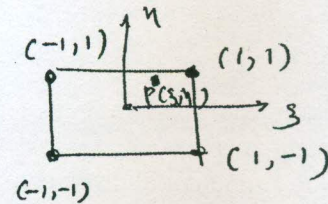


Fig.Q7(b)(ii)

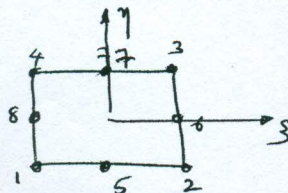


Fig.Q7(b)(iii)

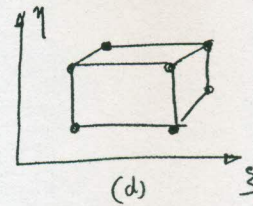


Fig.Q7(iv)

- 8 Write note on :
- Numbering of nodes
 - Patch test
 - Softwares used in FEM
 - Constitutive law.

(20 Marks)
